

# 1) THE FOREIGN EXCHANGE AND MONEY MARKET MODEL

## THE FOREIGN EXCHANGE MARKET

Exchange rate: The price of one currency in terms of another

Rate of return (RR)

(1)  $RR_{\$} = R_{\$}$  ← Expected depreciation

(2)  $RR_{\epsilon} = R_{\epsilon} + \frac{E^e - E}{E}$

(3)  $RR_{\$} = RR_{\epsilon}$

Endogenous:  $RR_{\$}$ ,  $RR_{\epsilon}$ ,  $E$

### Solving the model

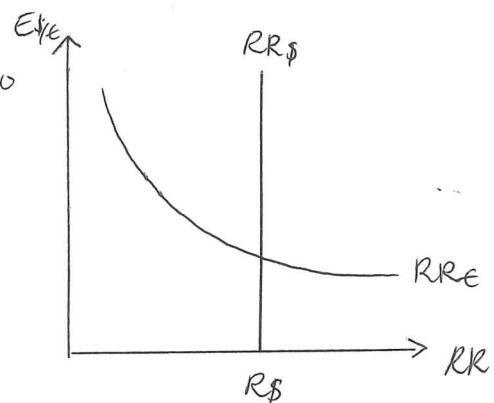
The uncovered interest parity condition (UIP)

$$R_{\$} = R_{\epsilon} + \frac{E^e - E}{E}$$

Finding the  $RR_{\$}$  curve from (1)

The equilibrium exchange rate (from UIP)

$$E = \frac{E^e}{1 + R_{\$} - R_{\epsilon}} \rightarrow \text{Find } \frac{\partial E}{\partial E^e} > 0, \frac{\partial E}{\partial R_{\$}} < 0, \frac{\partial E}{\partial R_{\epsilon}} > 0$$



Finding the  $RR_{\epsilon}$  curve from (2)

$$\frac{\partial RR_{\epsilon}}{\partial E} < 0 \text{ and } \frac{\partial^2 RR_{\epsilon}}{\partial E^2} > 0$$

→ Falling, convex curve

## THE MONEY MARKET

Money supply ( $\frac{M^s}{P}$ ) is given by the central bank

Money demand ( $\frac{M^d}{P}$ )

$$M^d = P \cdot L(R, Y)$$

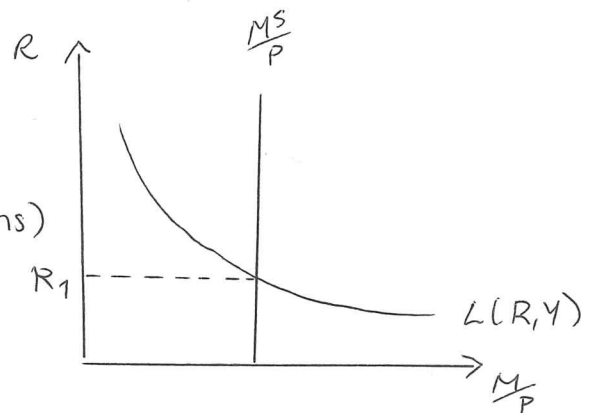
$$\Rightarrow \frac{M^d}{P} = L(R, Y)$$

Equilibrium  $M^s = M^d$  (for analytical solutions)  
→ Equilibrium interest rate  $R_1$

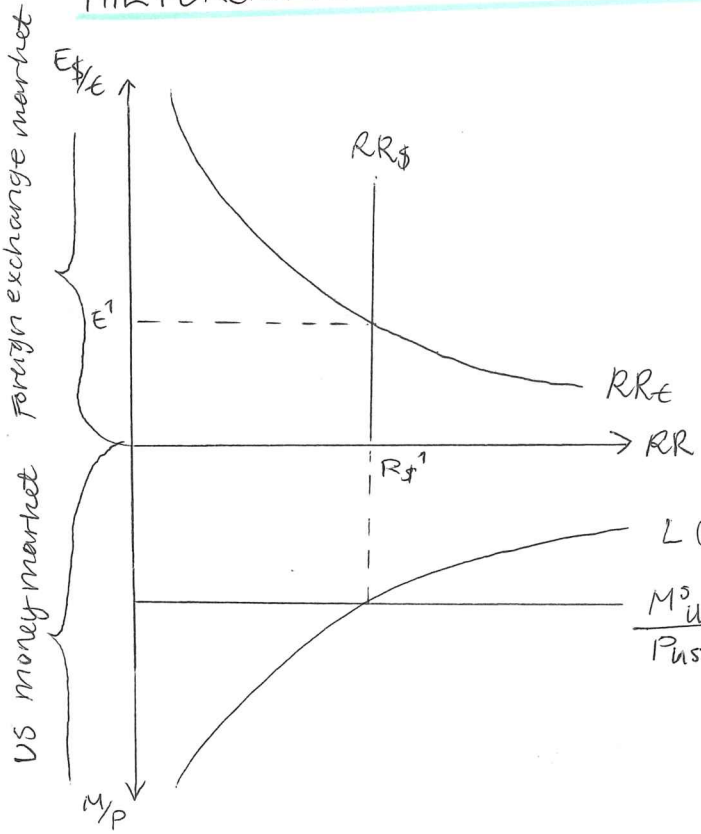
Assume

$$\frac{\partial M^d}{\partial R} < 0, \frac{\partial M^d}{\partial Y} > 0, \frac{\partial M^d}{\partial P} > 0$$

The demand for and price of bonds ensures equilibrium



# THE FOREIGN EXCHANGE AND MONEY MARKET MODEL



- Relationship between money supply and inflation

$$\frac{M^s}{P} = L(R, Y) \Rightarrow P = \frac{M^s}{L(R, Y)} \Rightarrow \frac{\Delta P}{P} = \frac{\Delta M^s}{M^s} - \frac{\Delta L}{L}$$

→ Assume that R and Y long run levels, so  $\frac{\Delta L}{L} = 0$

$$\frac{\Delta P}{P} = \frac{\Delta M^s}{M^s}$$

→ Inflation and money supply growth are equal in the long run

- Purchasing power parity (PPP)

$$E_{\$/\text{€}} = \frac{P_{us}}{P_{\text{€}}}$$

→ If PPP:  $P_{us} \uparrow \Rightarrow E_{\$/\text{€}} \uparrow$

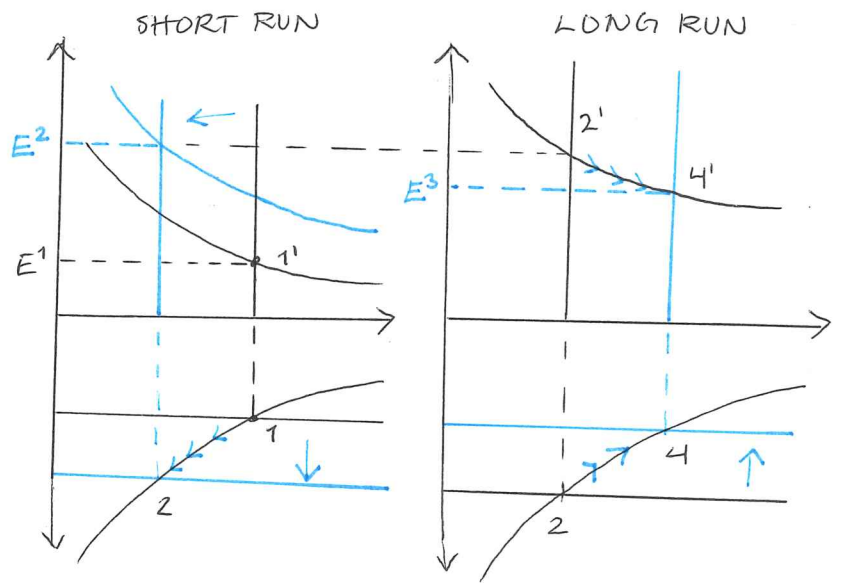
- Short-run and long-run effects of a permanent increase in money supply
  - short run:  $M^s \uparrow$  and  $E^e \uparrow$  (because  $E^e \uparrow$  when permanent increase)
  - Long run: Price level increases so  $M^s$  shifts back

- Exchange rate overshooting

→ New equilibrium exchange rate is depreciated, but not as much as initially

- Time paths of main variables

→  $M_{us}, R_{\$}, P_{us}, E_{\$/\text{€}}$



## 2) THE AA-DD MODEL

### DD-SCHEDULE: OUTPUT MARKET EQUILIBRIUM

- The DD schedule shows all combinations of output and the exchange rate where the output market is in equilibrium

- Finding the equation for aggregate demand:

Aggregate demand

$$D = C + I + G + CA$$

Consumption

$$C = C(Y - T)$$

Current account

$$CA = CA\left(\frac{EP^*}{P}, Y - T\right)$$

↳ Marshall-Lerner

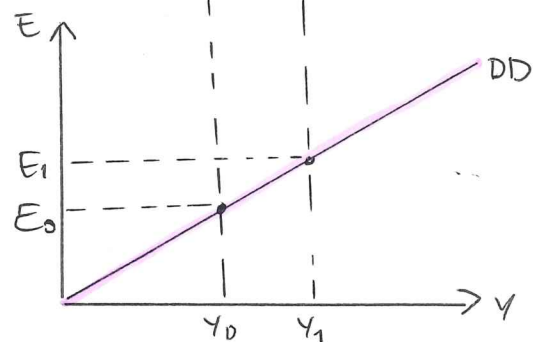
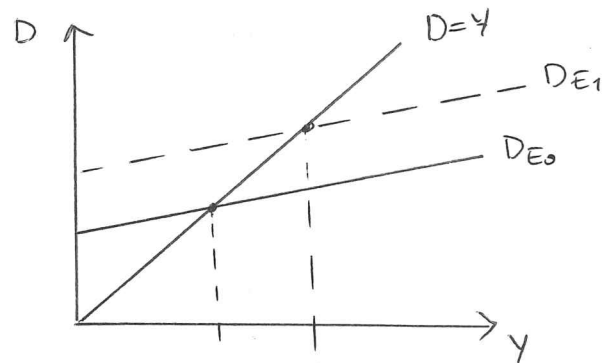
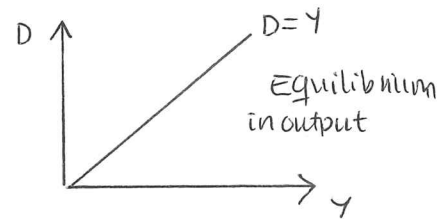
$$\Rightarrow Y = C(Y - T) + I + G + CA\left(\frac{EP^*}{P}, Y - T\right)$$

$$\Rightarrow D = D\left(\frac{EP^*}{P}, Y - T, I, G\right)$$

- We find the DD schedule by imagining  $E \uparrow$ , from  $E_0$  to  $E_1$  (assume  $P$  and  $P^*$  fixed)

→ Mechanism:  $E \uparrow \Rightarrow \frac{EP^*}{P} \uparrow \Rightarrow CA \uparrow \Rightarrow Y \uparrow$

- Outward shift:  $G \uparrow, T \downarrow, I \uparrow, P \downarrow, P^* \uparrow$



### AA-SCHEDULE: ASSET MARKET EQUILIBRIUM

- The AA schedule shows all combinations of output and the exchange rate where the domestic money market and the foreign exchange market are in equilibrium

- The money market equilibrium

$$\frac{M^s}{P} = L(R, Y)$$

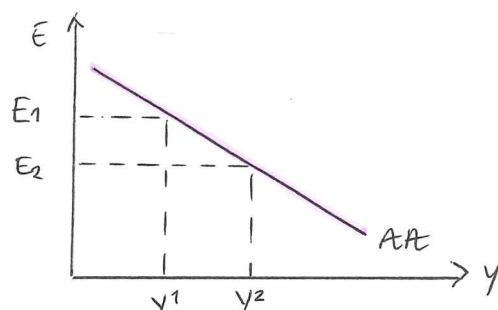
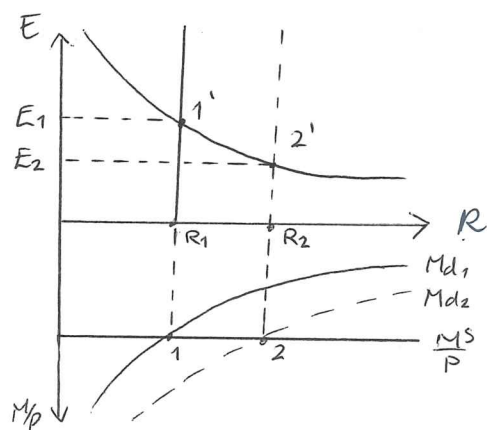
- The foreign exchange market equilibrium

$$R = R^* + \frac{E^e - E}{E}$$

- We find the AA schedule by imagining  $Y \uparrow$ , from  $Y^1$  to  $Y^2$

→ Mechanism:  $Y \uparrow \Rightarrow M^d \uparrow \Rightarrow R \uparrow \Rightarrow E \downarrow$

- Outward shift:  $M^s \uparrow, P \downarrow, E^e \uparrow, R^* \uparrow$



# THE AA-DD MODEL

(1)  $Y = C(Y-T) + I + G + CA(C \frac{EP^*}{P}, Y-T)$

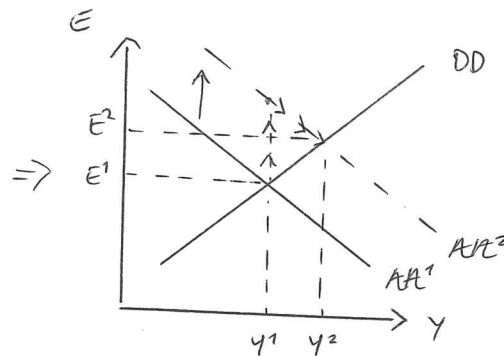
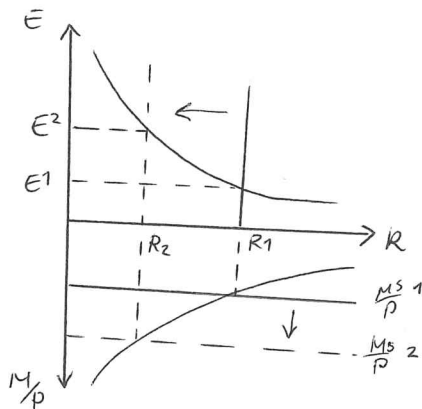
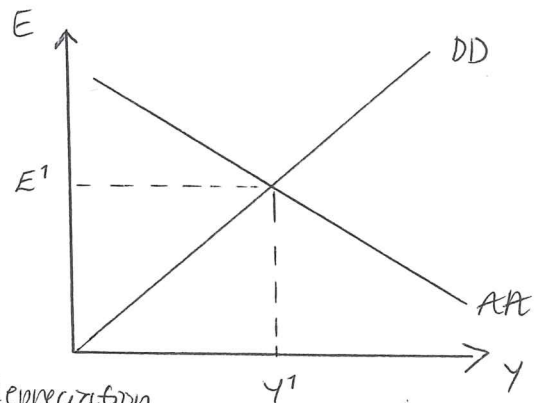
(2)  $\frac{M^s}{P} = L(R, Y)$

(3)  $R = R^* + \frac{E^c - E}{E}$

• Endogenous:  $Y, R, E$

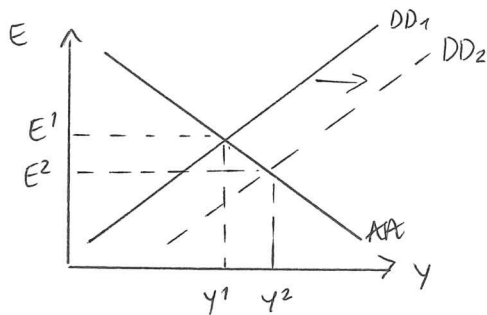
• Expansionary monetary policy,  $M^s \uparrow$ : Currency depreciation

→ Higher  $E$  for given  $Y$  in AA



• Expansionary fiscal policy,  $G \uparrow$ : Currency appreciation

→ Higher  $Y$  for given  $E$  in DD



• Fiscal vs. monetary policy: different effect on the current account

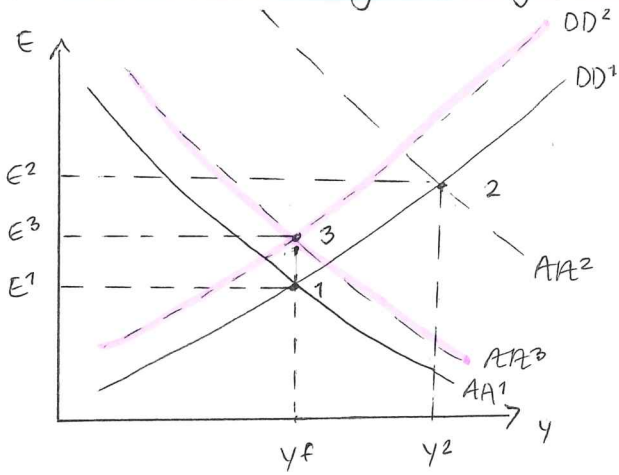
→ Monetary:  $M^s \uparrow \Rightarrow R \downarrow \Rightarrow E \uparrow \Rightarrow CA \uparrow$

→ Fiscal:  $G \uparrow \Rightarrow Y \uparrow \Rightarrow M^d \uparrow \Rightarrow R \uparrow \Rightarrow E \downarrow \Rightarrow CA \downarrow$

• The liquidity trap:  $R=0$

→ Monetary policy does not work

• Permanent expansionary monetary policy,  $M^S \uparrow$



→ First: AA shifts upwards ( $E^e \uparrow$ )

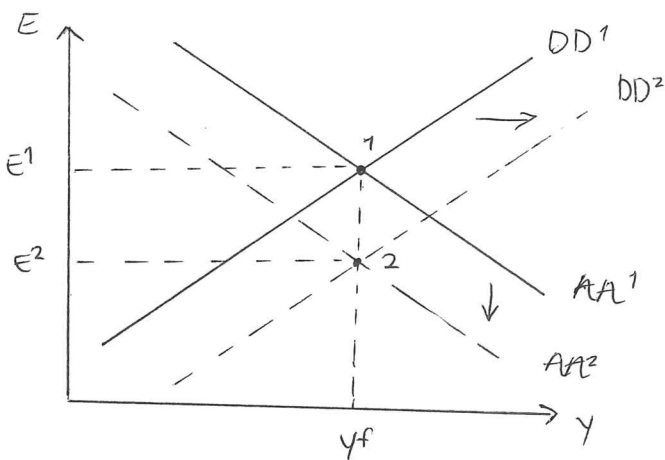
→ long run:  $P \uparrow$

DD:  $\frac{E P^*}{P} \downarrow \Rightarrow CA \downarrow \Rightarrow Y \downarrow$  (shift left)

AA:  $\frac{M^S}{P} \downarrow \Rightarrow R \uparrow \Rightarrow E \downarrow$  (shift down)

( $E^3 > E^1$  because  $E^e$  has increased)

• Permanent expansionary fiscal policy,  $G \uparrow$



→ DD shifts right

→ AA immediately shifts down because ( $E^e \downarrow$ )

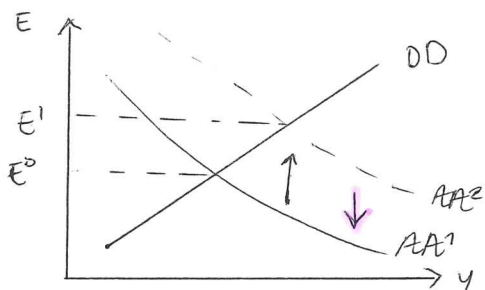
( $E^2$  is both short and long run equilibrium)

• Foreign exchange interventions: The central bank buys or sells foreign assets to affect its exchange rate (when fixed exchange rate to defend)

AA↓ → Selling foreign assets (→ pressure for depreciation) ⇒ Decreased money supply

AA↑ → Buying foreign assets (→ pressure for appreciation) ⇒ Increased money supply

• Monetary policy with fixed exchange rate

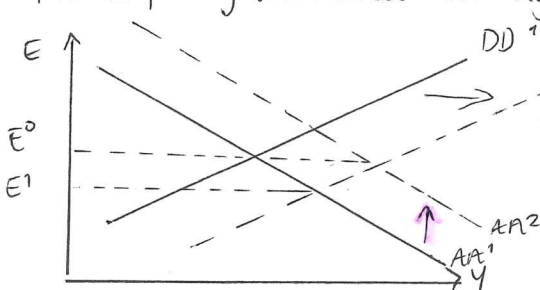


→ First: Monetary policy (AA upwards)

→ Then: Must sell foreign assets to keep  $E = E^0$  (AA shifts back)

Monetary policy does not work

• Fiscal policy with fixed exchange rate



→ First: Fiscal policy (DD right)

→ Then: Must buy foreign assets to keep  $E = E^0$  (AA shifts up)

Works, but we need sufficient reserves

### 3) MUNDELL'S MODEL FOR OPTIMAL CURRENCY AREAS (OCA)

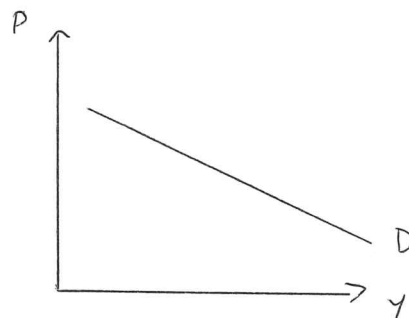
- Monetary union
  - common currency
  - common central bank
- A country in a monetary union is not able to:
  - Devalue/revalue its currency
  - Determine the quantity of national money in circulation
  - Change the short term interest rate

#### AGGREGATE DEMAND - AGGREGATE SUPPLY MODEL

- How to handle asymmetric shocks?
- Automatic adjustments
  - Wage flexibility
  - Labor mobility
- Economic policies
  - Monetary policy
  - Fiscal policy
- Demand curve

$$Y = F\left(\frac{M}{P}, G, T, \frac{EP^*}{P}, \alpha\right)$$

$\quad \quad \quad + \quad + \quad - \quad + \quad +$



- Mechanism
  - 1)  $P \uparrow \Rightarrow \frac{EP^*}{P} \downarrow \Rightarrow \text{Net exports} \downarrow \Rightarrow Y \downarrow$
  - 2)  $P \uparrow \Rightarrow \frac{M}{P} \downarrow \Rightarrow \text{Interest rate} \uparrow \Rightarrow \text{Investment} \downarrow \Rightarrow Y \downarrow$
- Outward shift

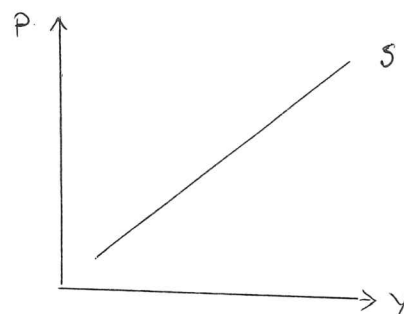
- |                                   |                               |                                    |                             |
|-----------------------------------|-------------------------------|------------------------------------|-----------------------------|
| $M \uparrow$                      | $G \uparrow, T \downarrow$    | $E \uparrow, P^* \uparrow$         | $\alpha \uparrow$           |
| $\underbrace{\hspace{2em}}$       | $\underbrace{\hspace{2em}}$   | $\underbrace{\hspace{2em}}$        | $\underbrace{\hspace{2em}}$ |
| Expansionary<br>monetary politics | Expansionary<br>fiscal policy | Real exchange<br>rate depreciation | Demand<br>shock             |

#### Supply curve

$$Y = G\left(\frac{W}{P}, \beta\right)$$

$\quad \quad \quad - \quad +$

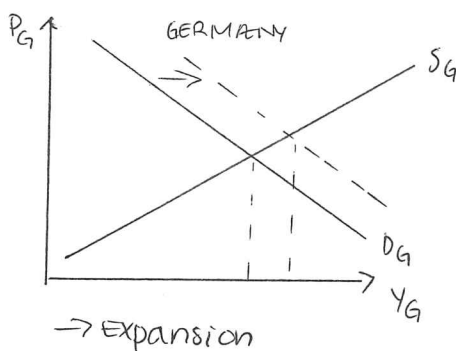
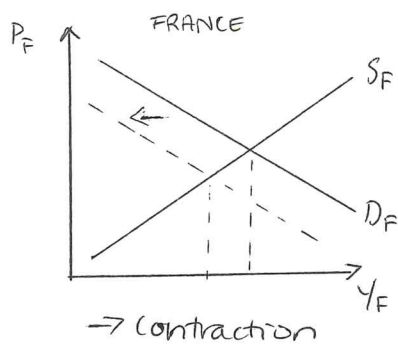
$\frac{W}{P}$  - real wage  
 $\beta$  - supply shock



- Mechanism:  $P \uparrow \Rightarrow \frac{W}{P} \downarrow \Rightarrow Y \uparrow$
- Outward shift:  $W \downarrow, \beta \uparrow$

# ASYMMETRIC SHOCKS IN A MONETARY UNION

- Asymmetric shock in aggregate demand

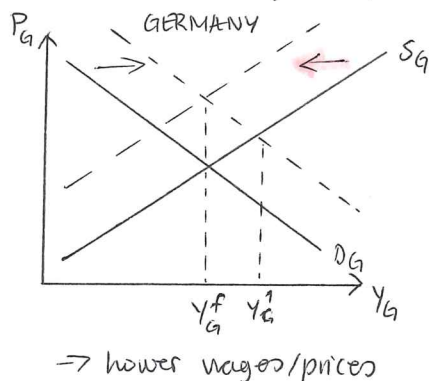
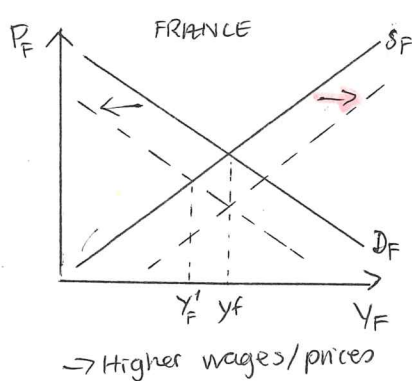


## Automatic adjustments

### Wage flexibility

→ France: Unemployment  $\Rightarrow$  Reduced wage claims  $\Rightarrow$  Positive supply shifts

→ Germany: Pressure in labour markets  $\Rightarrow$  Wages are pushed up  $\Rightarrow$  Negative supply shift



### Labor mobility

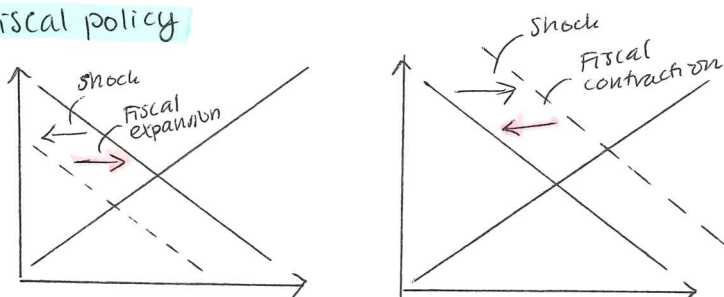
→ Unemployed workers in France move to Germany

## Economic policies

### Monetary policy

→ France needs expansion, Germany needs restriction  $\Rightarrow$  Does not work

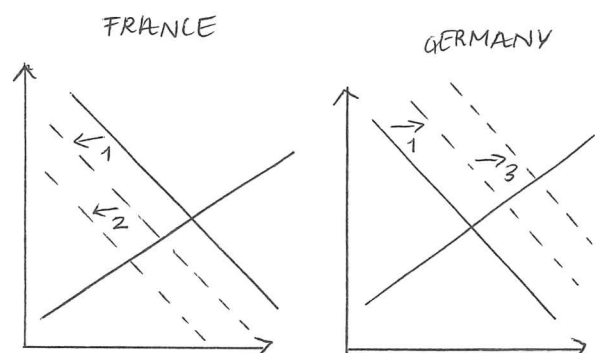
### Fiscal policy



## Debt dynamics

- Asymmetric shocks
- French budget deficit increase  $\Rightarrow$  Capital outflow, interest rate  $\uparrow$
- Capital inflow to Germany  $\Rightarrow$  interest rate  $\downarrow$

- Initial shocks are strengthened by the debt crisis in France



# 1) THE BARRO-GORDON MODEL

## EXPECTATIONS-AUGMENTED PHILLIPS CURVE

• Phillips curve

$$\dot{p} = \dot{p}^e - \frac{1}{\alpha} (u - u_N)$$

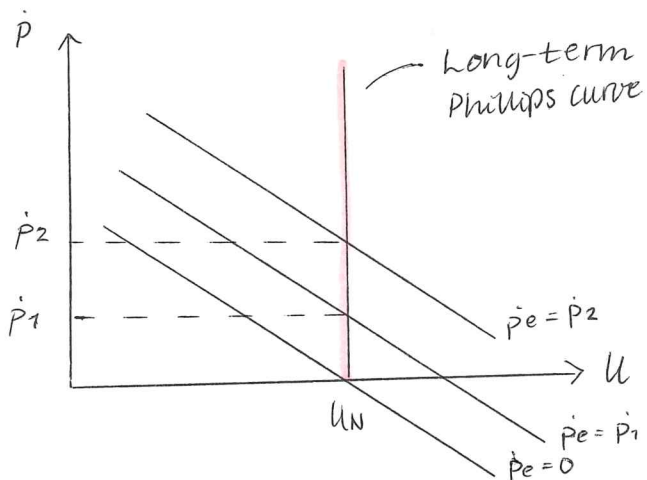
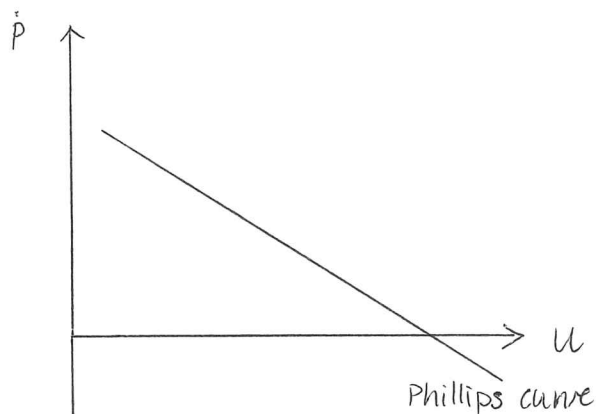
$u$  - unemployment rate  
 $u_N$  - natural rate of  $u$   
 $\dot{p}$  - inflation  
 $\dot{p}^e$  - expected inflation

• Trade off between inflation and unemployment

$$\rightarrow u \downarrow \Rightarrow W \uparrow \Rightarrow P \uparrow \Rightarrow \dot{p} \uparrow$$

• Long-term Phillips curve

$$\rightarrow \text{Rational expectations: } u = u_N \Rightarrow \dot{p} = \dot{p}^e$$



## PREFERENCES OF THE MONETARY AUTHORITIES

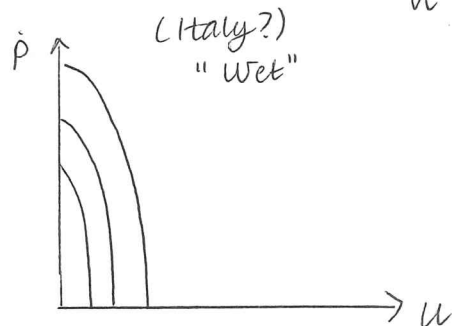
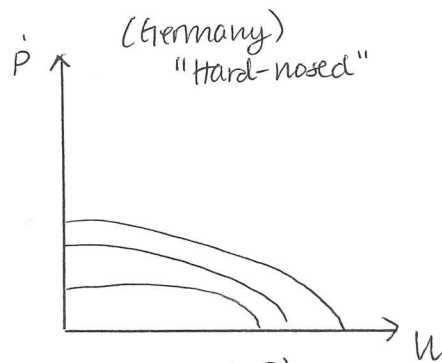
• Welfare function of government

$$V = V(u, \dot{p})$$

• Closer to origin  $\rightarrow$  lower welfare loss

• "Hard-nosed" government: care relatively more about inflation

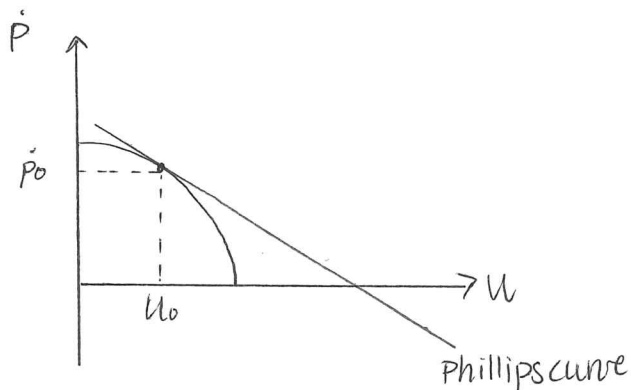
• "Wet" government: care relatively more about unemployment



## SHORT RUN EQUILIBRIUM

• Lowest indifference curve given the Phillips curve

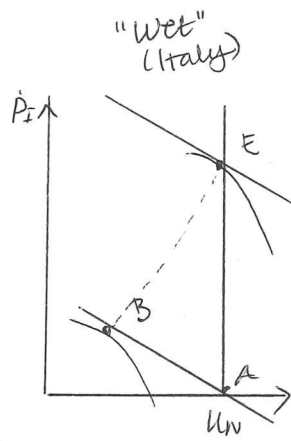
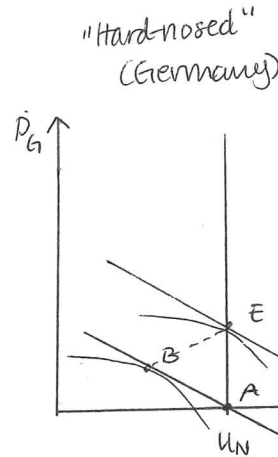
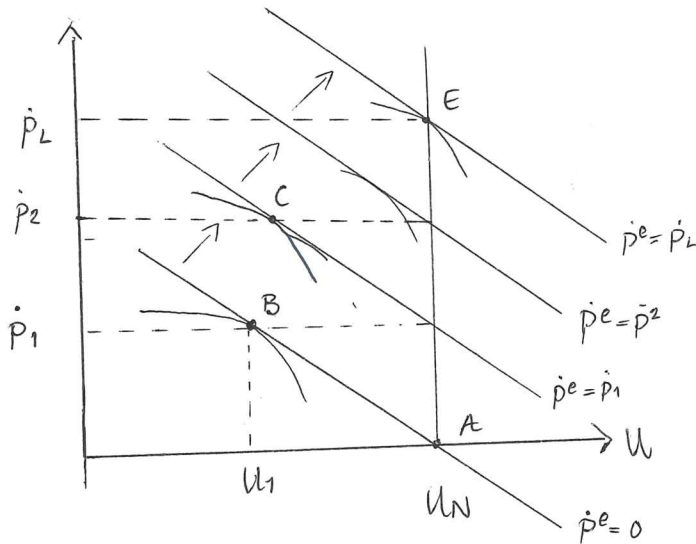
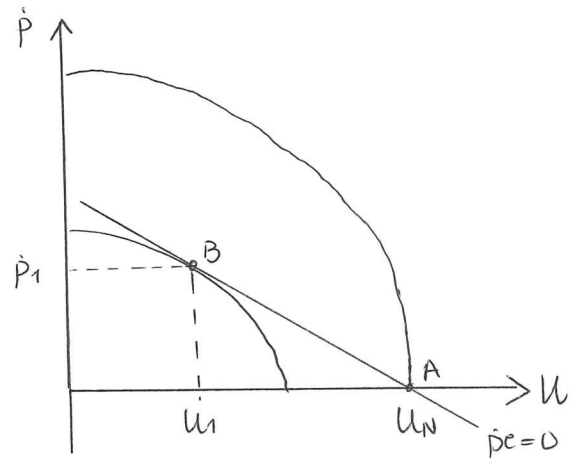
$\rightarrow$  sets  $\dot{p}_0$  with interest rate, gets  $u_0$





# LONG RUN EQUILIBRIUM

- Start in A with  $\dot{p}^* = 0$ 
  - The monetary policy is credible, so  $\dot{p}^e = 0$
- Incentive to generate surprise inflation
  - Reach B with higher utility
- Over time, inflation expectations are adjusted upwards
  - B → C → → E (long run equilibrium)
  - This process is called **stagflation**



- The equilibrium level of inflation depends on the preferences of the authorities
  - Italy has high preference for low unemployment, but ends up with  $U_N$  and high inflation
  - $E = \dot{P}_I - \dot{P}_G \Rightarrow$  Depreciation of the Italian currency

## SOLUTION: MONETARY UNION WITH SAME CURRENCY

- Control high inflation in countries with wet governments and unstable exchange rates
- Italy will convince citizens that point F is credible
- Issue: central bank represented by both preferences:

$$\Rightarrow \dot{p}_G < \dot{p}_{\text{union}} < \dot{p}_I$$

- Low inflation country loses welfare, high inflation country gains welfare

